Enhancement of Thermoelectric Properties by Modulation-Doping in Silicon Germanium Alloy Nanocomposites

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ABSTRACT: Modulation-doping was theoretically proposed and experimentally proved to be effective in increasing the power factor of nanocomposites (Si80Ge20)(Si100B5)30 by increasing the carrier mobility but not the figure-of-merit (ZT) due to the increased thermal conductivity. Here we report an alternative materials design, using alloy Si70Ge30 instead of Si as the nanoparticles and Si95Ge5 as the matrix, to increase the power factor but not the thermal conductivity, leading to a ZT of 1.3 ± 0.1 at 900 °C.

KEYWORDS: Modulation-doping, thermoelectrics, nanocomposite, silicon germanium (SiGe), dimensionless figure-of-merit

The performance of thermoelectric materials depends on their dimensionless thermoelectric figure-of-merit ZT = (Sσ/κ)T, where S is the Seebeck coefficient, σ the electrical conductivity, κ the thermal conductivity, and T the absolute temperature at which the properties are measured. The numerator Sσ is called the power factor. It is generally recognized that for the next generation of thermoelectric materials, strategies to enhance the power factor are essential in addition to those to decrease the thermal conductivity.

Silicon germanium (SiGe) alloys are suitable candidates for high-temperature thermoelectric applications because of their reasonably good thermoelectric properties and superior long-term reliability at elevated temperatures. Consequently, SiGe thermoelectric modules with a material ZT of 0.5 (p-type) and 0.9 (n-type) have been used in space radioisotope thermoelectric generators (RTGs) by United States NASA since 1976. New applications, especially heat conversion at high temperatures, demand higher ZTs for such material applications. Recently, a good enhancement in ZT values has been demonstrated for both n- and p-type SiGe alloys by using a nanocomposite approach. The lattice thermal conductivity of the nanocomposite samples is much lower compared to that of their equivalent large crystalline bulk materials because of the much increased grain boundaries of the numerous nanograins that effectively scatter long wavelength phonons. Using this approach, the peak ZT value of p-type nanostructured Si80Ge20B5 samples was improved from 0.5 to 0.95, and that of n-type Si80Ge20P from 0.93 to around 1.3. However, these materials contain a fairly high concentration of Ge that is about a hundred times more expensive than Si. In 2009, Zhu et al. reported that by using the nanocomposite approach, only a 5% Ge replacement of Si is sufficient to further reduce the thermal conductivity of n-type nano-Si by a factor of 2, resulting in a ZT peak value of 0.94 in Si80Ge20 doped with GaP and P at ~900 °C, and this result is significant since a much smaller amount of expensive Ge is used. Furthermore, if Ge is entirely eliminated, the ZT peak of pure nano-Si would drop to about 0.7 at around 1000 °C. Clearly there is a trade-off between the cost and the performance of Si1−xGex alloys.

Recently, we introduced a three-dimensional (3-D) modulation-doping approach to improve the power factor of thermoelectric nanocomposites by mainly increasing the carrier mobility. Modulation-doping has been widely used in thin-film semiconductors that separate the charge carriers from the ionized dopants to reduce the charge scattering and to increase the carrier mobility, thus increasing the electrical conductivity as a consequence. The proposed modulation-doped sample is a two-phase nanocomposite made out of two different types of nanograins. Rather than uniformly doping the sample, dopants are incorporated into only one type of nanograins. Charge carriers spill over from the doped nanograins to the undoped or lightly doped matrix phase, leaving behind ionized nanograins. Instead of the usually heavy uniform doping in thermoelectric materials, causing strong ionized impurity scattering of charges, ionized nanoparticles can be spatially placed much further apart in the modulation-doping scheme, leading to reduced electron scattering for higher mobility. Traditionally, molecular beam epitaxy (MBE) was used to grow these thin layers, consisting of an undoped conducting layer (channel), a doped layer that donates carriers, and an undoped spacer layer separating the ionized dopants from the conducting channel. Adapting such a concept, our study theoretically and experimentally demonstrated that...
modulation-doping is also effective in 3-D bulk nanocomposite systems by improving the mobility, thus the power factor. The power factor of the p-type Si$_{80}$Ge$_{20}$B$_{5}$ uniform sample was improved by 40% using the modulation-doping approach achieved by using a 30% fraction of Si$_{80}$Ge$_{20}$ nanograins in the intrinsic Si$_{80}$Ge$_{20}$ matrix to make a modulation-doped sample: (Si$_{80}$Ge$_{20}$)$_{0.3}$(Si$_{80}$Ge$_{20}$)$_{0.7}$. A smaller improvement of about 20% was observed in the power factor of a n-type sample (Si$_{80}$Ge$_{20}$)$_{0.3}$(Si$_{80}$P$_{3}$)$_{0.7}$ compared to its equivalent uniform nanocomposite Si$_{80}$Ge$_{20}$P$_{3}$. However, the ZTs were not increased due to the high thermal conductivities of the pure Si nanoparticles.

The modulation-doping scheme produced enhancement in electrical conductivity, leading to the increase in the electronic part of the thermal conductivity. Such an increase in the electronic part is inevitable because charge carriers are also heat carriers. At the same time, the increase in the lattice part is also unavoidable since the nanoparticles Si have a much higher thermal conductivity. Ideally, we want to maintain the low thermal conductivity of the nanostructured materials. Therefore modulation-doping scheme should be also focused on strategies to reduce the lattice part of the thermal conductivity. Here, we report our success on simultaneously improving the power factor and reducing the lattice part of the thermal conductivity by a new materials design and band alignment in the scheme of modulation-doping by using Si$_{80}$Ge$_{20}$ as the matrix (instead of Si$_{80}$Ge$_{20}$ lower Ge concentration not only increase the mobility but also reduce the cost) and Si$_{80}$Ge$_{20}$P$_{3}$ as the nanoparticles that have a much lower thermal conductivity, to eventually enhance the ZT.

Ideally, for modulation-doping in bulk nanocomposites, one wants to choose nanoparticles with a low density of states compared to the matrix. The nanoparticles should also form proper band alignments with the matrix to promote the flow of carriers from the nanoparticles into the matrix. In this study, we have chosen Si$_{80}$Ge$_{20}$P$_{3}$ as the doped nanoparticle for two reasons: good band alignment and low thermal conductivity. It is known that SiGe and Si can form either type I or type II band alignment in thin-film heterostructures (Figure 1). In nanocomposites, it is difficult to determine the band alignment because such composites are obtained by consolidating two types of crystal grains into a bulk 3-D material instead of growing atomic layers one by one. Both types of grains might be under tension, and the possible dangling bonds, impurities, and trapped charges at the interfaces might all affect the final band alignment. For n-type materials, the nanoparticles should have relatively higher conduction band edges compared to the matrix grains, forcing the carriers to flow into the matrix for our materials design, we accept type II band alignment, which is the case for the Si/Ge interface, and therefore we chose nanoparticle grains containing more Ge compared to the matrix. From our experimental observations, which will be shown later, one can conclude that the band discontinuity in our case is type II and is large enough for the purpose of modulation-doping. Moreover, a larger density of states effective mass (mainly due to the larger valley degeneracy of Si compared to Ge) in the Si-rich matrix (Si$_{80}$Ge$_{20}$) compared to the selected nanoparticles leads to more available energy states for the carriers to fill.

For the consideration of the thermal conductivity, Si$_{80}$Ge$_{20}$ has the lowest thermal conductivity among Si$_{80}$Ge$_{20}$ alloys. Using Si$_{80}$Ge$_{20}$P$_{3}$ composition as the nanoparticles then has clearly a big advantage in our experiment; as we increase the nanoparticle molar fraction, the thermal conductivity decreases and the electrical conductivity increases simultaneously.

The alloyed Si$_{80}$Ge$_{20}$ nanopowders were prepared by ball milling pure elements of Si, Ge, and P for about 10 h in a high-energy ball mill and then mixed in the container according to the designed molar ratio for a very short time (several minutes). Finally the powder mixtures were consolidated rapidly into 12.7 mm disks in a graphite die by a dc hot press method. The sample density was measured by the Archimedes method, and all samples reported here have densities close to the theoretical values (Table 1). We measured the electrical conductivity and the Seebeck coefficient using a commercial four-probe system (ULVAC, ZEM-3) and using 2 × 2 × 12 mm bars cut from the disks. The thermal diffusivity was measured directly on these disks by laser flash (NETZSCH LFA 457), and the specific heat was measured by differential scanning calorimetry (DSC, NETZSCH 404C). All experiments were repeated a few times, and the data are within the measurement errors (3% for electrical conductivity, thermal diffusivity, and specific heat, 4% for thermal conductivity, and 5% for Seebeck coefficient, resulting in an uncertainty of 11% for the ZT values). Room temperature Hall measurements were performed on polished thin bulk samples using a physical properties measurement system (PPMS) from Quantum Design with typical sample dimensions of 0.5 × 2 × 11 mm. The hot-pressed samples were also cut, polished, and then ion milled for microstructure study using transmission electron microscopy (TEM, JEOL JSM2010F) techniques.

We study the thermoelectric properties of the proposed modulation-doped (Si$_{100}$B$_{5}$)$_{1-x}$(Si$_{80}$Ge$_{20}$P$_{3}$)$_{x}$ as a function of nanoparticle molar fraction, x. For comparison purposes, we also prepared composition equivalent uniform samples as

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**Table 1. Theoretical and Measured Densities of As-Prepared Silicon Germanium Nanocomposite Samples**

<table>
<thead>
<tr>
<th>sample type</th>
<th>modulation doped (NPs molar fraction)</th>
<th>equivalent uniform</th>
<th>uniform</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>5% 15% 25% 35% 45%</td>
<td>5% 15% 25% 35% 45%</td>
<td>Si$<em>{80}$Ge$</em>{20}$P$_{3}$</td>
</tr>
<tr>
<td>theoretical (g cm$^{-3}$)</td>
<td>2.517 2.592 2.666 2.741 2.816</td>
<td>2.517 2.592 2.666 2.741 2.816</td>
<td>2.480</td>
</tr>
<tr>
<td>measured (g cm$^{-3}$)</td>
<td>2.505 2.596 2.662 2.731 2.813</td>
<td>2.511 2.590 2.671 2.728 2.815</td>
<td>2.482</td>
</tr>
<tr>
<td>percentage (%)</td>
<td>99.5 100.2 99.8 99.6 99.9</td>
<td>99.8 99.9 100.2 99.5 100.0</td>
<td>100.1</td>
</tr>
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**Figure 1.** Type I (strained SiGe on Si) and type II (strained Si on SiGe) band alignments.
references: Si_{93.75}Ge_{6.25}P_{1.05} Si_{91.25}Ge_{8.75}P_{0.45} Si_{88.75}Ge_{11.25}P_{0.75} Si_{86.25}Ge_{13.75}P_{1.05} and Si_{83.75}Ge_{16.25}P_{1.35}. Figure 2a shows the electrical conductivity at room temperature as a function of Ge concentration. In modulation-doped samples, a fairly good electrical conductivity $\sigma$ of $9.25 \times 10^4$ S m$^{-1}$ is achieved with even only 5% nanoparticles and $\sigma$ continues to rise with increasing nanoparticle ratio. When we increase the molar fraction of nanoparticles, more carriers are introduced into the matrix to increase the electrical conductivity through modulation-doping. However, at the same time, these nanoparticles also introduce excessive interfaces and a larger static potential barrier (when compared to ionized impurity atoms) to scatter the electrons, which negatively affect the electrical conductivity. So when the nanoparticle molar fraction increases to more than 35%, the electrical conductivity starts to decrease, as shown in Figure 2a. Similar trends are observed in the equivalent samples. However, for the equivalent samples, the electrical conductivity starts to decrease, when the nanoparticle molar fraction increases to more than 35%, the electrical conductivity starts to decrease, while the carrier concentration stays almost the same at around $2.78 \times 10^{20}$ cm$^{-3}$ in both samples. Surprisingly, the mobility of the modulation-doped samples is also higher than that of $29.21$ cm$^2$ V$^{-1}$ s$^{-1}$ of the uniform nanocomposite Si$_{86.25}$Ge$_{13.75}$P$_{1.05}$ (optimally doped matrix) that has much less Ge, further proving the advantage of our current materials designing approach.

For the thermal conductivity $\kappa$ (Figure 2b), unlike our previous study$^{10}$ in which the thermal conductivity increased largely with the addition of nanoparticles (pure Si was used), here it is natural that $\kappa$ rapidly goes down as the ratio of nanoparticles increases, since the doped nanoparticles are less thermally conductive than the matrix. The lowest room temperature thermal conductivity reaches about $3.90$ W m$^{-1}$ K$^{-1}$ at the highest nanoparticle molar ratio (45%), equivalent to a composition of Si$_{83.75}$Ge$_{16.25}$P$_{1.35}$. Comparing to the equivalent uniform sample, modulation-doped samples have higher electronic thermal conductivities because of their higher electrical conductivities. For example, for the 45% volume fraction of nanoparticles, the electronic part of the thermal conductivity is around $1$ W m$^{-1}$ K$^{-1}$ using the Wiedemann-Franz law assuming a Lorenz number of $2.44 \times 10^{-8}$ W Ω K$^{-2}$, while that of the equivalent sample is only $0.7$ W m$^{-1}$ K$^{-1}$. In this study, we were able to maintain the total thermal conductivity of the modulation-doped sample as low as those of the single-phase equivalent samples, which means that the lattice part of the thermal conductivity in our modulation-doped nanocomposite sample is lower than its equivalent single-phase sample.

Figure 2c shows the ratio $\sigma/\kappa$ (at room temperature) dependence of the Ge concentration. It is clearly shown that the $\sigma/\kappa$ ratio of the modulation-doped samples increases much faster than those of the equivalent uniform samples with increasing Ge content. In fact, most of the rapid increase in $\sigma/\kappa$ is from the rapid increase in the electrical conductivity (Figure 2a), while the values of the thermal conductivities (Figure 2b) are comparable, which is very different from the situation when pure Si was used as the nanoparticle material. The highest $\sigma/\kappa$ value for our modulation-doped samples happens at 35% nanoparticles, or 13.75% Ge equivalently, which is 54% higher than the $\sigma/\kappa$ of its equivalent uniform nanocomposite Si$_{86.25}$Ge$_{13.75}$P$_{1.05}$.

Figure 3 shows the temperature dependence of the thermoelectric properties of modulation-doped samples. This figure shows that the increase of the electrical conductivity (Figure 3a) decreases the Seebeck coefficient (Figure 3b) due to the usual interdependence of the transport parameters. The obvious trend of the lower thermal diffusivity and thermal conductivity (Figure 3c,e, respectively) is caused by the interface phonon scattering due to the presence of more nanoparticles. The low thermal conductivity also benefits from the low specific heat (Figure 3d) of the nanoparticles. With 35% nanoparticles, our modulation-doped sample has the biggest advantage on the $\sigma/\kappa$ value over its equivalent uniform sample (Figure 2c), and the highest ZT value reaches 1.3 at 900 °C (Figure 3f), about the same as that of the best uniform nanocomposite Si$_{86.25}$Ge$_{13.75}$P$_{1.05}$ reported for Si$_{1−x}$Ge$_x$ so far, but data$^{10}$ with a similar composition, indicating that the current materials design is more favorable for n-type Si$_{1−x}$Ge$_x$ samples. We should point out that the mobility of our best sample with 35% nanoparticles at room temperature is 36.42 cm$^2$ V$^{-1}$ s$^{-1}$, which is much higher compared to its uniform counterpart Si$_{86.25}$Ge$_{13.75}$P$_{1.05}$ with a mobility of $24.26$ cm$^2$ V$^{-1}$ s$^{-1}$, while the carrier concentration stays almost the same at around $2.78 \times 10^{20}$ cm$^{-3}$ in both samples.
less Ge is used in the modulation-doped samples, meaning lower cost.

Figure 4 shows the comparison for each individual property between the best modulation-doped sample \((\text{Si}_{95}\text{Ge}_{5})_{0.65}(\text{Si}_{70}\text{Ge}_{30}\text{P}_{3})_{0.35}\) and its equivalent uniform sample \(\text{Si}_{86.25}\text{Ge}_{13.75}\text{P}_{2}\). To compare the modulation-doping with uniform impurity doping, we also include the data for the optimally doped matrix, \(\text{Si}_{95}\text{Ge}_{5}\text{P}_{2}\). As one could see, over the whole temperature range, the modulation-doped sample has a higher electrical conductivity due to higher carrier mobility than the equivalent uniform sample (Figure 4a). The difference is pretty large at low temperature but gets smaller as the temperature increases, since electron-phonon scattering increases with temperature and starts to dominate at high temperatures.\(^{1}\) Another possibility is that the interfaces may also have a larger impact on carrier transport at high temperatures. Compared to the modulation-doped sample, the uniform \(\text{Si}_{95}\text{Ge}_{5}\text{P}_{2}\) sample has a much higher carrier concentration of \(4.01 \times 10^{20} \text{cm}^{-3}\) at room temperature due to its higher P concentration, which should be the reason for its higher electrical conductivity even though its carrier mobility is lower. The modulation-doped sample has a similar thermal diffusivity (Figure 4d) and a similar specific heat \(C_v\) values (Figure 4e) compared to the equivalent uniform sample. As a result, the thermal conductivity (Figure 4f) of the modulation-doped sample is similar to that of the equivalent uniform sample. However the temperature dependence of \(\sigma/k\) (Figure 4g), clearly shows that the modulation-doped sample has an advantage over the whole temperature range. It is important to note that the Seebeck coefficient of any modulation-doped sample in our study is similar to that of its corresponding equivalent uniform sample, similar to our observations in the previous report.\(^{10}\) For example in Figure 4b, considering the 5% experimental error bar, the values for Seebeck coefficient are very close over the whole temperature range. Overall, our modulation-doping approach has improved the value of \(\sigma/k\) but has left the Seebeck coefficient almost untouched. With higher electrical conductivity and a similar Seebeck coefficient, the modulation-doped sample shows an improved power factor compared to its equivalent uniform sample, leading to the fact that the modulation-doped sample shows better ZT values (Figure 4h) than the equivalent uniform sample. Because the absolute ZT value at low temperature is small, one may find the difference at low temperature insignificant. Actually, the improvement at room temperature is 23%. At 900 °C, the peak value is close to 1.3, about 30% higher than the equivalent uniform sample \((\text{ZT} \sim 1.0)\) and 36% higher than the optimally doped matrix \((\text{ZT} \sim 0.9)\). Comparing to the previously reported best n-type alloy \(\text{Si}_{95}\text{Ge}_{5}\text{P}_{2}\), the peak ZTs are basically the same, but the modulation-doped samples contain much less Ge, equivalent to \(\text{Si}_{86.25}\text{Ge}_{13.75}\text{P}_{1.05}\) meaning a much lower fabrication cost.

Since the matrix and nanoparticles have different Si to Ge ratios, they may diffuse into each other during the hot-pressing.
process. To prove whether such diffusion has really happened, we performed an energy dispersive spectroscopy (EDS) study on our hot-pressed modulation-doped samples using a TEM. For reference purposes, Si$_{95}$Ge$_5$ nanopowders were measured first. The EDS data repeatedly showed that the average atomic ratio between Si and Ge is 94.3:5.7, which is very close to the as-prepared composition (95:5). After the validation step, we then measured the best modulation-doped samples with a 35% nanoparticle molar fraction. At low magnifications (30 000–100 000) with the incident beam spread over a larger sample area, EDS results showed that the average chemical composition of the area is Si$_{86}$Ge$_{14}$, consistent with the designed equivalent composition Si$_{86.25}$Ge$_{13.75}$. At higher magnification (Figure 5a,b), we found that there are two typical domains with different compositions. The ones with more Si (Figure 5a), with the measured Si:Ge at five positions to be 89.1:10.9 (A), 89.3:10.7 (B), 89.4:10.6 (C), 89.3:10.7 (D), and 90.9:9.1 (E), give an average value of 89.6:10.4, which indicates 5% diffusion of Ge from nanoparticles into the matrix when compared to the original matrix composition of 95:5. The other domains turn out to have higher Ge (Figure 5b): 73.1:26.9 (A), 69.3:30.7 (B), 75.1:24.9 (C), and 75.1:24.9 (D), giving an averaging 73.1:26.9, little bit higher Si than that of the nanoparticles Si$_{70}$Ge$_{30}$P$_3$, a result of the minor diffusion. Typical EDS spectra for each case are given in Figure 5c. From these results, we could say that even though there might be some diffusion between the matrix and the nanoparticles, the two

Figure 4. Temperature-dependent (a) electrical conductivity $\sigma$, (b) Seebeck coefficient $S$, (c) power factor, (d) diffusivity, (e) specific heat $C_p$, (f) thermal conductivity $\kappa$, (g) $\sigma/\kappa$ ratio, and (h) ZT of modulation-doped Si$_{1-x}$Ge$_x$ nanocomposite sample with a 35% nanoparticle molar fraction, in comparison with those of equivalent uniform Si$_{86.25}$Ge$_{13.75}$P$_{1.05}$ and optimally doped Si$_{95}$Ge$_5$P$_2$ uniform samples.

Figure 5. (a-b) TEM images and (c) EDS spectra [the spectrum in (c) is for the grain E in (a), the inset in (c) is for the grain A in (b)] of modulation-doped sample with a 35% nanoparticle molar fraction.
components still keep apart from each other. Compared to a thin-film configuration of modulation-doped structures, a better design will be to have a spacer layer. The spacer would have a dual role. First it will prevent grain growth, and second, it will separate the carriers from their parent atoms. The spacer itself should not react with either the host or the nanoparticles. In n-type configuration, the case of this study, the spacer band should align below the nanoparticles band and above the host matrix, so that the carriers can fall from the nanoparticles to the spacer and then to the matrix. However, how to make those spacer layers turns out to be extremely challenging in nanocomposites. Nevertheless, modulation-doping behavior is successfully demonstrated in this work.

In conclusion, we designed a new materials approach to unambiguously demonstrate the effectiveness of modulation-doping in thermoelectric nanocomposites. The electrical conductivity of a Si$_{80.25}$Ge$_{13.75}$P$_{1.05}$ sample was improved by 54% using the modulation-doping approach in (Si$_{80}$(Ge$_{30}$)$_{5}$Si$_{30}$Ge$_{30}$P$_{3.35}$)$_{5}$ that has the same overall composition. The enhancement was due to the 50% enhancement of the carrier mobility by spatially separating carriers from their parent atoms. More importantly, the thermal conductivity was kept low due to the low thermal conductivity of the nanoparticles. In fact the two-phase composite has a lower lattice thermal conductivity compared to its equivalent single-nanoparticles. In fact the two-phase composite has a lower thermal conductivity produces a peak ZT of $\sim 30$ at 900 °C at 900 °C. To further improve the modulation-doping approach, using a thin spacer layer to minimize the diffusion would be expected to further improve the measured performance.

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Notes
The authors declare no competing financial interest.

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The resulted ZT is about 30